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Sixth Semester B.E. Degree Examination, June/July 2014
Operations Research

Time: 3 hrs.

Max. Marks: 100

**Note: Answer FIVE full questions, selecting
at least TWO questions from each part.**

PART - A

- 1 a. What is Operations Research? Mention six phases of an operations research study. (05 Marks)
- b. A farmer has 1,000 acres of land on which he can grow corn, wheat or soyabeans. Each acre of corn costs ₹100 for preparation, requires 7-mandays of work and yields a profit of ₹30. An acre of wheat costs ₹120 to prepare, requires 10-mandays of work and yields a profit of ₹40. An acre of soyabeans costs ₹70 to prepare, requires 8-mandays of work and yields a profit of ₹20. If the farmer has ₹1,00,000 for preparation and can count on 8,000 mandays work, formulate the L.P. model to allocate the number of acres to each crop to maximize the total profit. (08 Marks)
- c. Using Graphical method solve the LPP :
 Maximize $Z = 5x_1 + 4x_2$
 Subject to $6x_1 + 4x_2 \leq 24$
 $x_1 + 2x_2 \leq 6$
 $-x_1 + x_2 \leq 1$
 $x_2 \leq 2$; $x_1, x_2 \geq 0$ (07 Marks)
- 2 a. Define the following terms:
 (i) Slack variable (ii) Surplus variable (iii) Artificial variable. (06 Marks)
- b. Write six key solution concepts of simplex method. (06 Marks)
- c. Solve the problem using simplex method.
 Maximize $Z = 4x_1 + 3x_2 + 6x_3$
 Subject to $2x_1 + 3x_2 + 2x_3 \leq 440$
 $4x_1 + 3x_3 \leq 470$
 $2x_1 + 5x_2 \leq 430$; $x_1, x_2, x_3 \geq 0$ (08 Marks)
- 3 a. Use Big-M method and solve the problem:
 Maximize $Z = 3x_1 - x_2$
 Subject to $2x_1 + x_2 \leq 2$
 $x_1 + 3x_2 \geq 3$
 $x_2 \leq 4$; $x_1, x_2 \geq 0$ (10 Marks)
- b. Use the two-phase simplex method to
 Maximize $Z = 5x_1 - 4x_2 + 3x_3$
 Subject to $2x_1 + x_2 - 6x_3 = 20$
 $6x_1 + 5x_2 + 10x_3 \leq 76$
 $8x_1 - 3x_2 + 6x_3 \leq 50$; $x_1, x_2, x_3 \geq 0$ (10 Marks)
- 4 a. Use revised simplex method to solve the LPP.
 Maximize $Z = 2x_1 + x_2$
 Subject to $3x_1 + 4x_2 \leq 6$
 $6x_1 + x_2 \leq 3$; $x_1, x_2 \geq 0$ (12 Marks)
- b. Explain the key relationships between primal and dual problem. (08 Marks)

PART – B

- 5 a. Explain the of duality theory in sensitivity analysis. (06 Marks)
 b. In brief, explain the dual simplex method. (06 Marks)
 c. Illustrate the upper bound technique:

Maximize $Z = 2x_1 + x_2 + 2x_3$

Subject to $4x_1 + x_2 = 12$

$- 2x_1 + x_3 = 4$

and $0 \leq x_1 \leq 4, 0 \leq x_2 \leq 15, 0 \leq x_3 \leq 6$ (08 Marks)

- 6 a. Given below is the time required (in days) when a particular software program module is assigned to a particular programmer.

		Programmers			
		A	B	C	D
Modules	1	12	10	8	9
	2	8	9	11	7
	3	11	14	12	10
	3	9	9	8	9

Assign the modules to different programmers in such a way that the total computing time is least. (10 Marks)

- b. Solve the following travelling salesman job.

		To city				
		1	2	3	4	5
From city	1	-	10	25	25	10
	2	1	-	10	15	2
	3	8	9	-	20	10
	4	14	10	24	-	15
	5	10	8	25	27	-

(10 Marks)

- 7 a. Solve the following game with the payoff matrix (08 Marks)

		Player B			
		B ₁	B ₂	B ₃	B ₄
Player A	A ₁	1	7	3	4
	A ₂	5	6	4	5
	A ₃	7	2	0	3

- b. Solve the following 2 × 3 game graphically (12 Marks)

		Player B		
		B ₁	B ₂	B ₃
Player A	A ₁	1	3	12
	A ₂	8	5	2

- 8 Explain briefly:

- a. Metaheuristics, its nature, advantage and disadvantage.
 b. Minimum spanning tree problem with constraints
 c. Tabu search algorithm
 d. Genetic algorithm. (20 Marks)
